

Digital Image Processing

Feature Based Morphing Using Lines

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Lecture Objectives

- Previously
 - Interpolation
 - Warping
 - Morphing
- Today
 - Feature Based Morphs
 - Details of using line pairs

Morphing

- A smooth transition from one shape and coloring to another
- An image morph involves
 - warping both images to some intermediate shape such that they can be superimposed on each other
 - blending the two images together to produce a third image

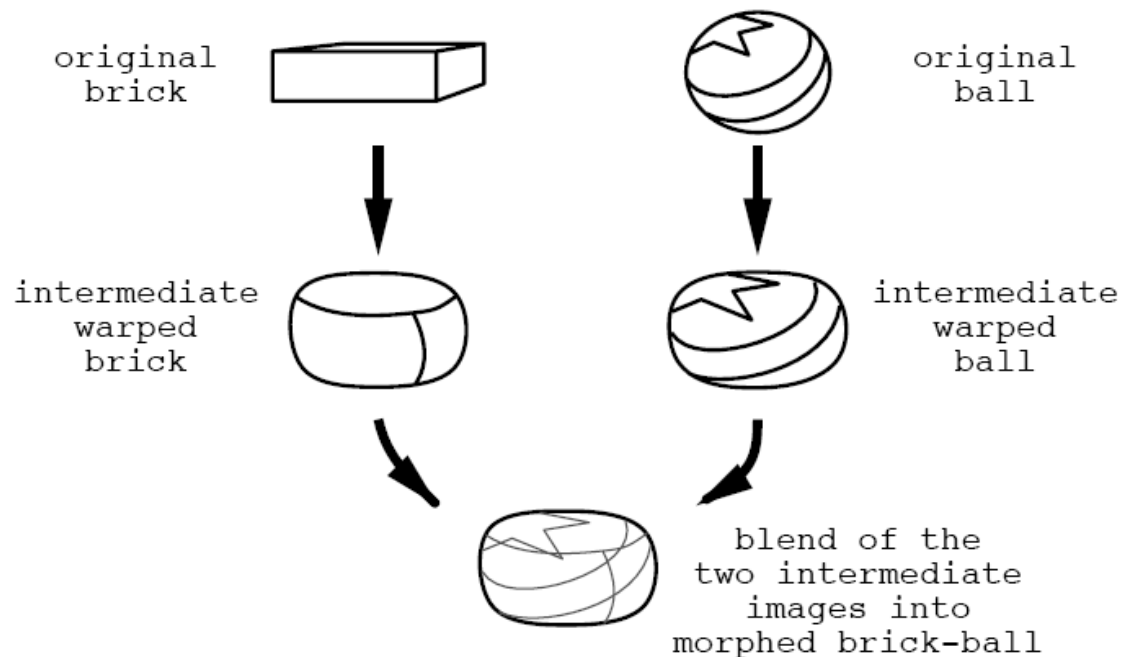


Figure 13.1: A Step in a Morph of a Brick into a Ball

Sample Steps

- Blend is controlled by giving more strength to the original image that is closer to the deformed shape

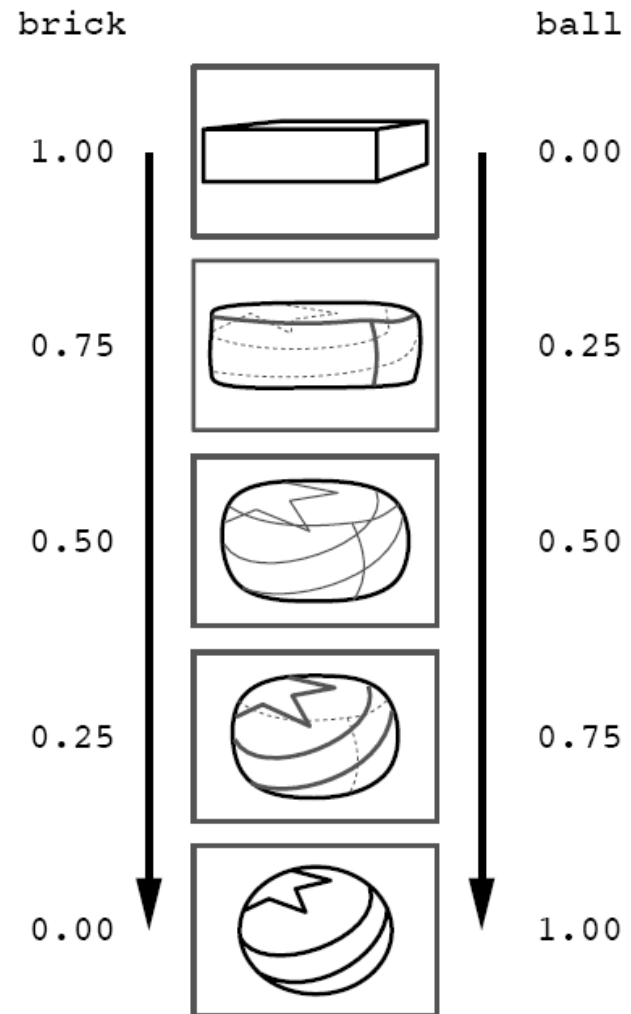


Figure 13.2: Steps in Morph Sequence from Brick to Ball

Feature-based Image Metamorphosis

- Concept:
 - Morph one image into another using an inverse map by specifying corresponding features in both images using directed lines

Beier, T & Neely, S. (1992). Feature-based image metamorphosis
Computer Graphics 26 (2): 35-42. doi: 10.1145/133994.134003

-- Identify features via line-pairs

3 Examples: Each Using One Pair of Lines

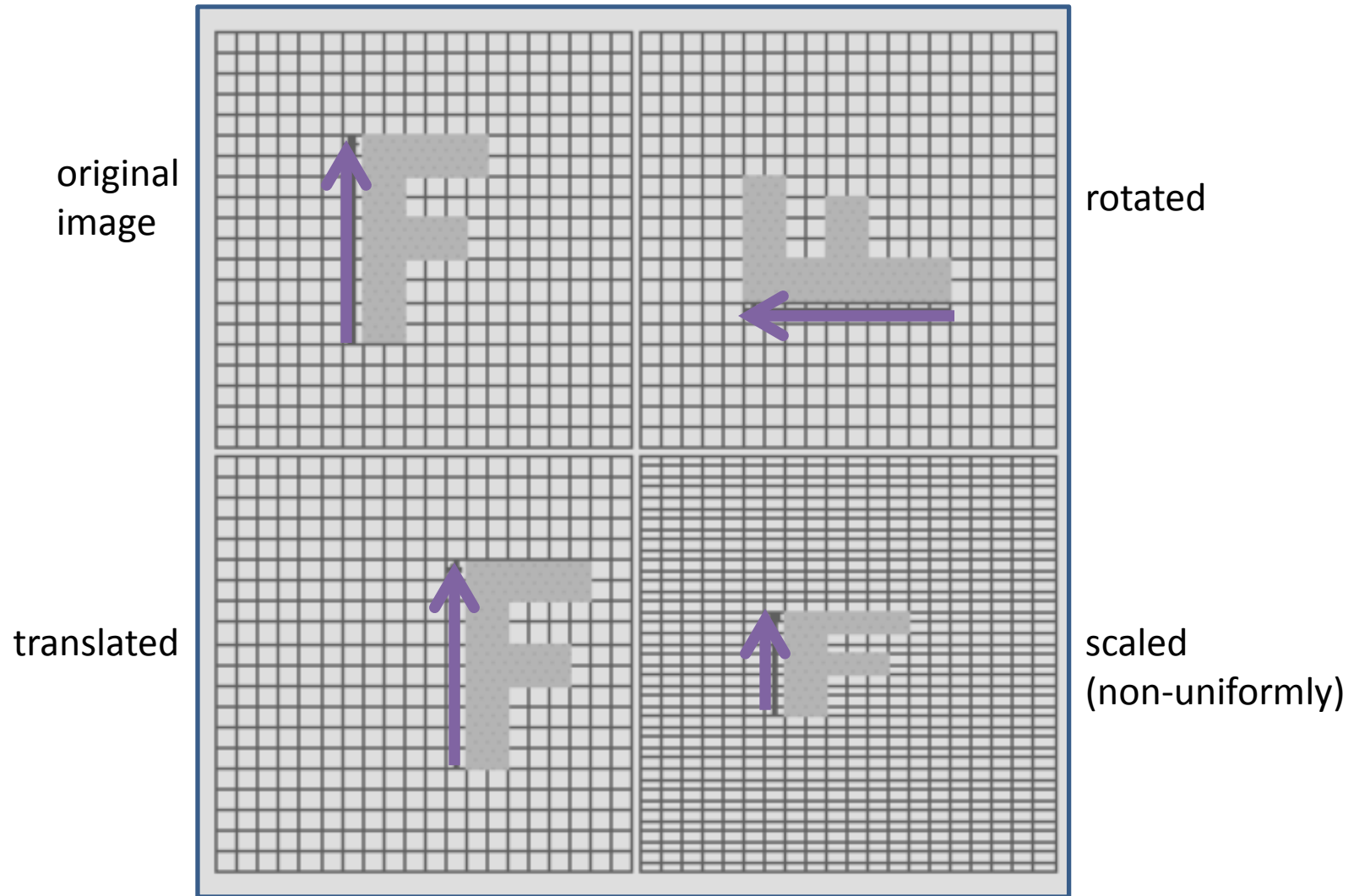
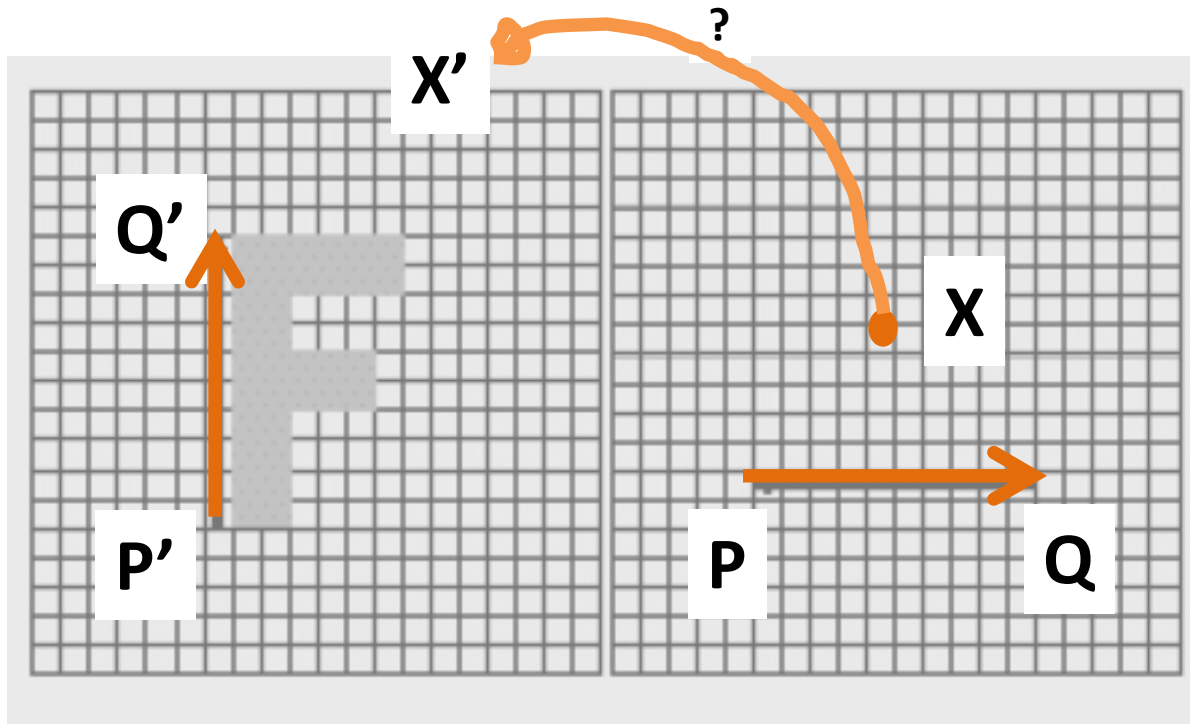


Figure 2: Single line pair examples

Transform via 1 pair of lines

- Given a line pair: PQ and $P'Q'$
 - Determine which pixel X' in the source image do we sample for the X pixel in the destination image



Transform via 1 pair of lines

- Solution Design

```
For each pixel  $X$  in the destination image
  find the corresponding  $u, v$ 
  find the  $X'$  in the source image for that  $u, v$ 
destinationImage( $X$ ) = sourceImage( $X'$ )
```

First:

Calculate parameters u and v

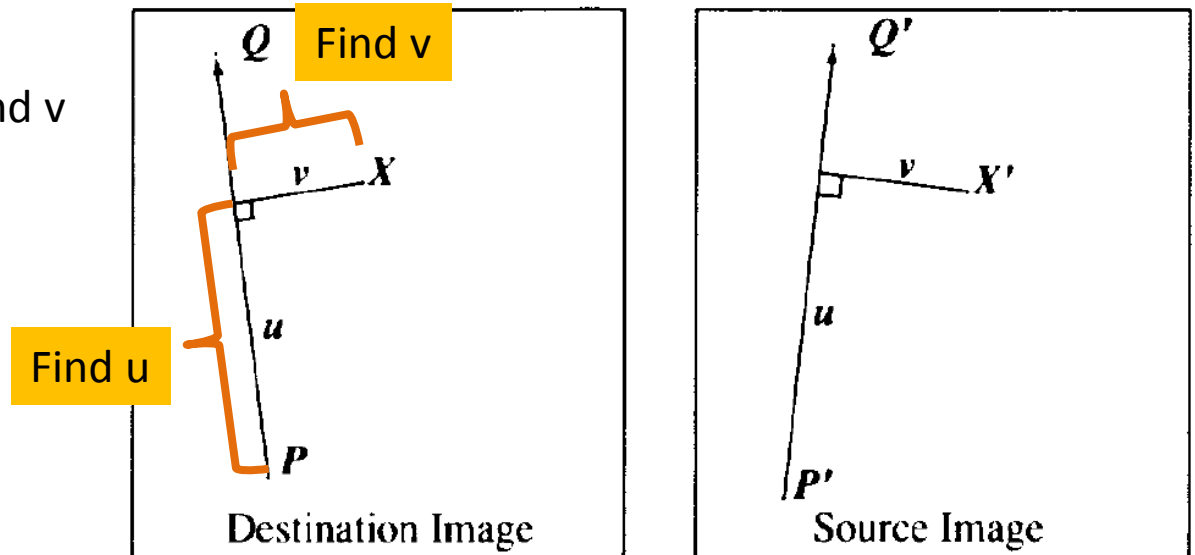


Figure 1: Single line pair

Transform via 1 pair of lines

- Solution Design

```
For each pixel X in the destination image  
  find the corresponding u, v  
  find the X' in the source image for that u, v  
destinationImage(X) = sourceImage(X')
```

First:

Calculate parameters u and v

Then

Use u, v to get X'

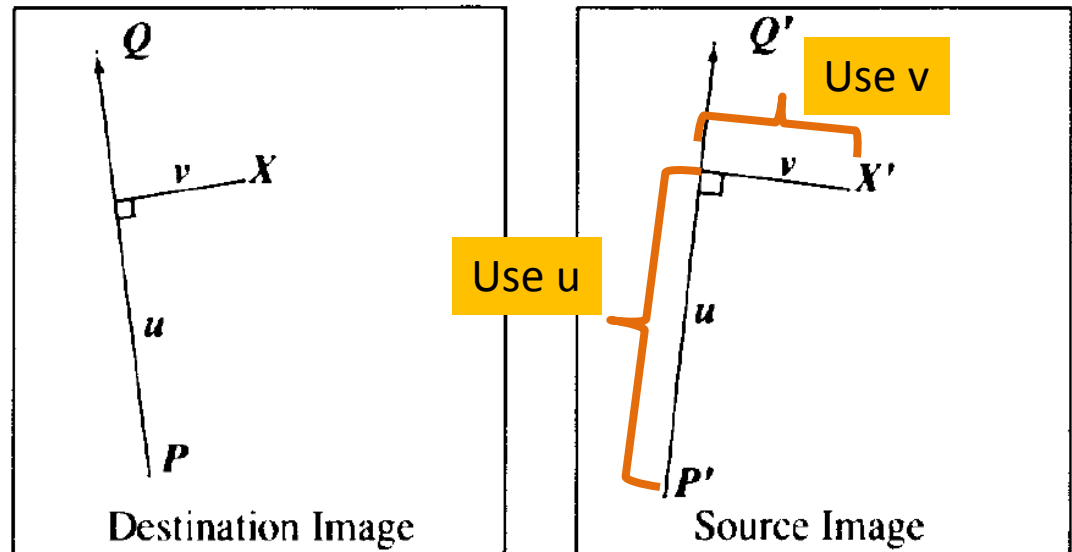
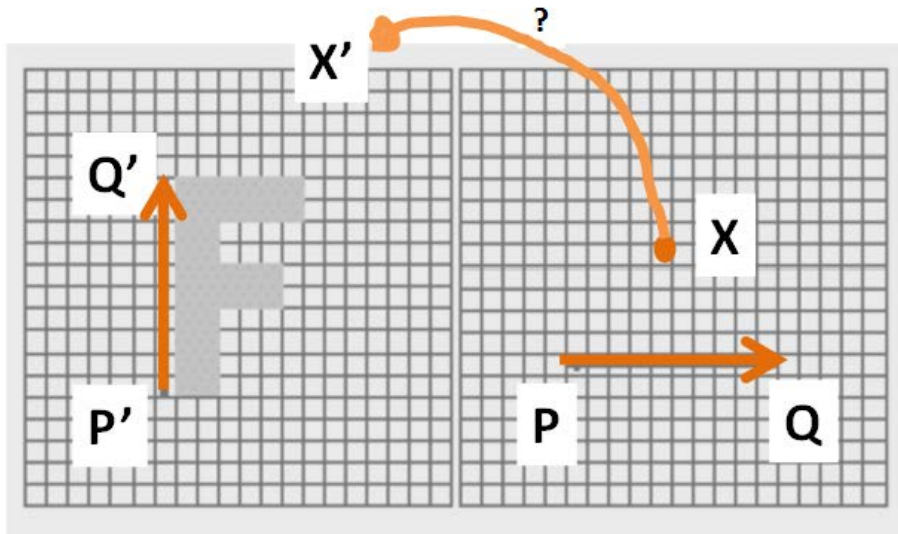


Figure 1: Single line pair

Implementation



$$u = \frac{(X - P) \cdot (Q - P)}{\|Q - P\|^2} \quad (1)$$

walk-thru of this follows

$$v = \frac{(X - P) \cdot \text{Perpendicular}(Q - P)}{\|Q - P\|} \quad (2)$$

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|} \quad (3)$$

Walk-Thru

$$u = \frac{(X - P) \cdot (Q - P)}{\|Q - P\|^2}$$

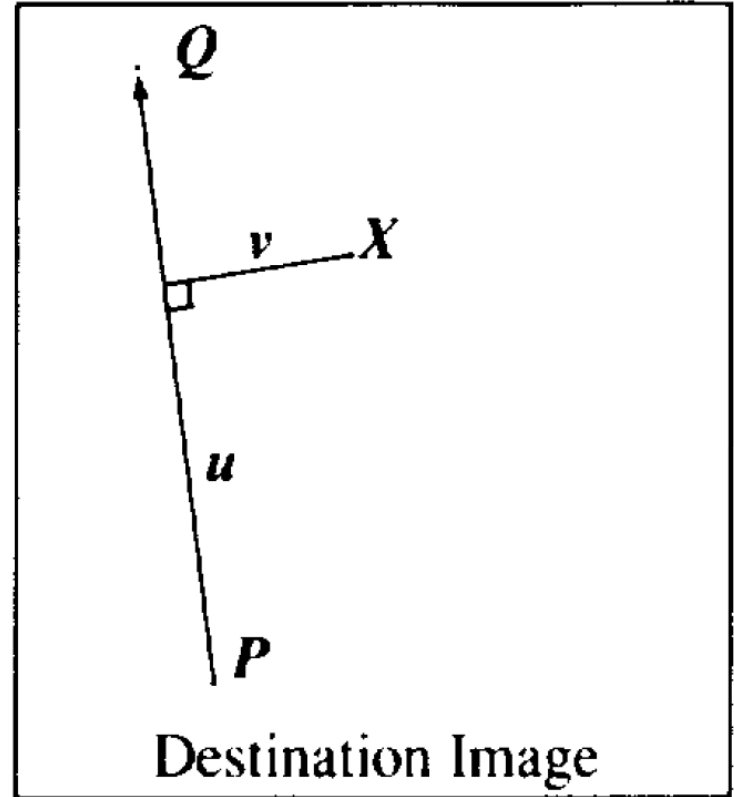
dot product and L2 norm

Example of Dot Product

$$(3,2) \cdot (4,5) = (3 * 4) + (2 * 5) = 12 + 10$$

L2 norm

is the length/magnitude of the vector



Walk-Thru

$$u = \frac{(X - P) \cdot (Q - P)}{\|Q - P\|^2}$$

dot product and L2 norm

In words:

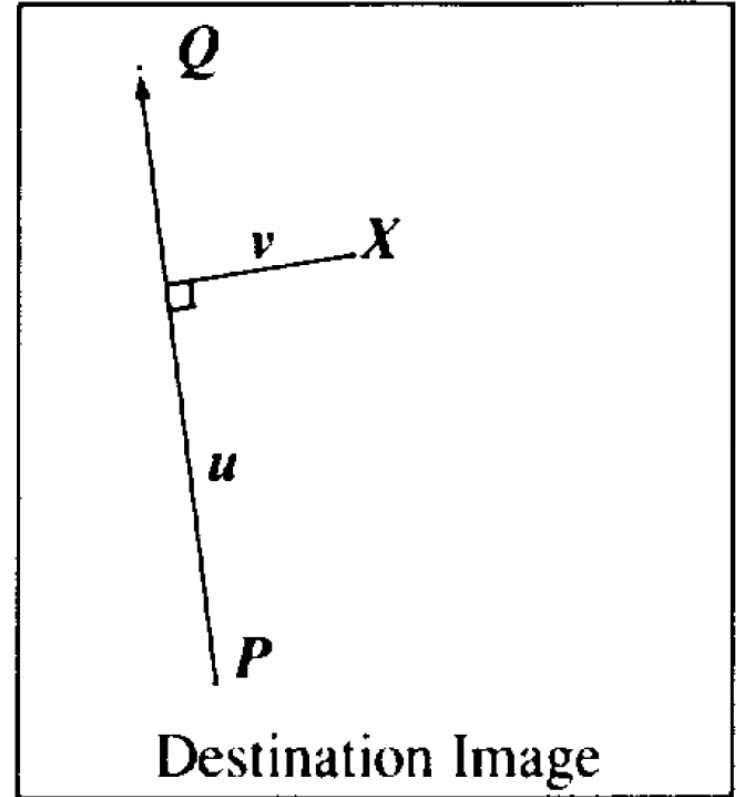
u is the position along the line PQ

u is a fraction

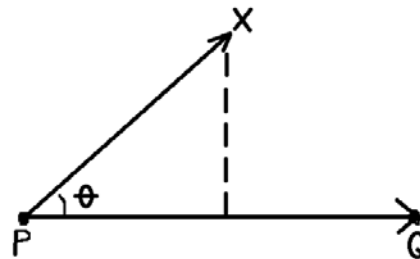
like a time parameter

u = 0 → P

u = 1 → Q



*u gives position of X
projected onto line PQ*



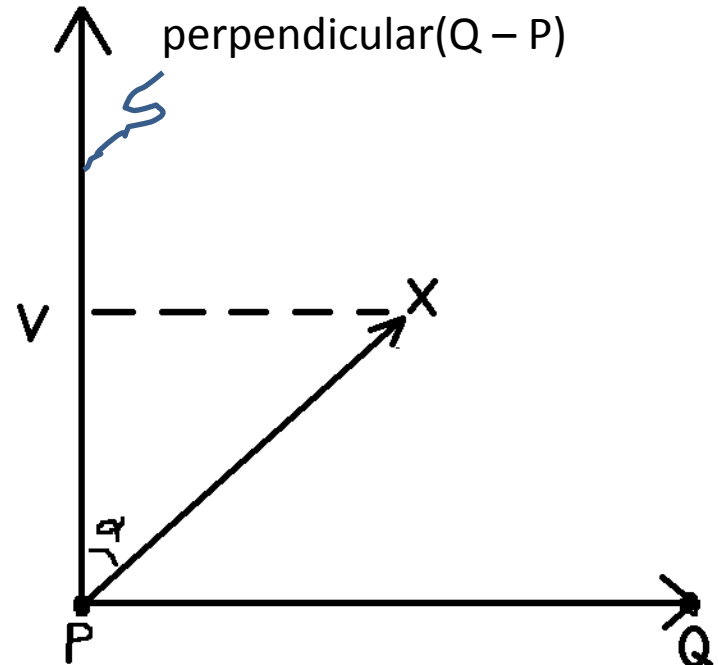
$$u = \frac{|PX| |PQ| \cos \theta}{|PQ| |PQ|}$$

Walk-Thru

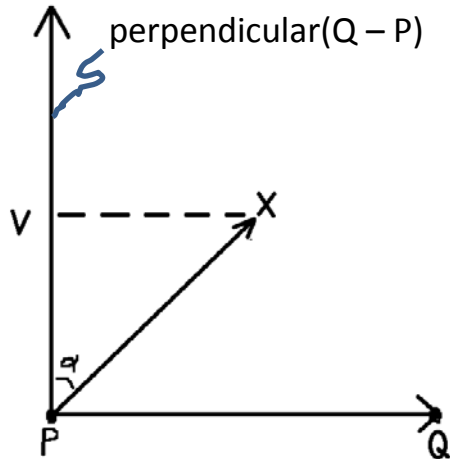
$$v = \frac{(X - P) \cdot \text{Perpendicular}(Q - P)}{\|Q - P\|}$$

Perpendicular()

returns the vector perpendicular to,
and the same length as, the input vector



Aside Example: Application of Transforms



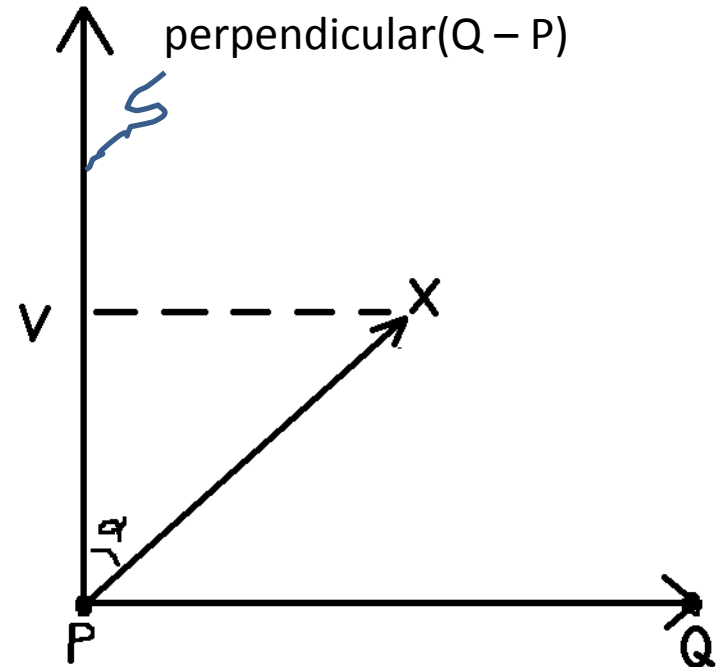
Calculation of Perpendicular(PQ)

assume P is (0, 0) and Q at (x, y)

$$\begin{bmatrix} \cos \frac{\pi}{2} & -\sin \frac{\pi}{2} \\ \sin \frac{\pi}{2} & \cos \frac{\pi}{2} \end{bmatrix} \overrightarrow{PQ} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -y \\ x \end{bmatrix}$$

Walk-Thru

$$\begin{aligned}v &= \frac{(\mathbf{X} - \mathbf{P}) \cdot \text{Perpendicular}(\mathbf{Q} - \mathbf{P})}{\|\mathbf{Q} - \mathbf{P}\|} \\ &= \frac{|PX| |\text{perpendicular}(PQ)| (\cos\alpha)}{|PQ|} \\ &= |PX| (\cos\alpha)\end{aligned}$$



v is NOT normalized = distance in pixels from the PQ line

Walk-Thru

Using u and v , we now compute X'

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|}$$

Walk-Thru

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$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|}$$

$$= P' + u \cdot (P'Q') + v \left(\underbrace{\frac{\text{perpendicular}(P'Q')}{|P'Q'|}} \right)$$

note: this is a unit vector

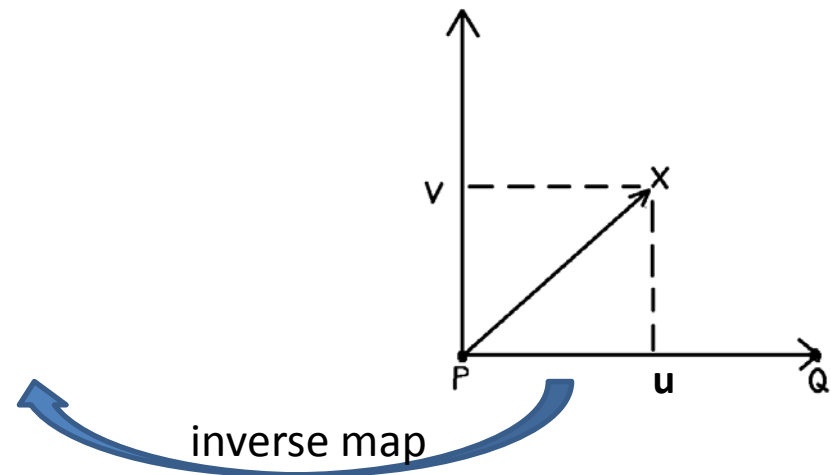
Walk-Thru

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note: this is a unit vector



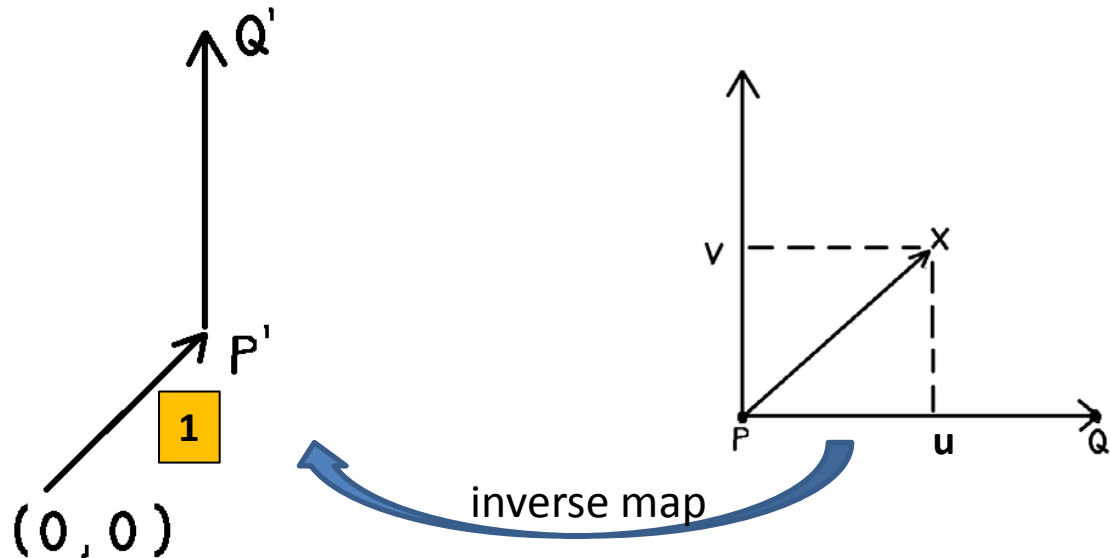
Walk-Thru

Using u and v , we now compute X'

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|}$$

$$= P' + u \cdot (P'Q') + v \left(\underbrace{\frac{\text{perpendicular}(P'Q')}{|P'Q'|}}_1 \right)$$

note: this is a unit vector



Walk-Thru

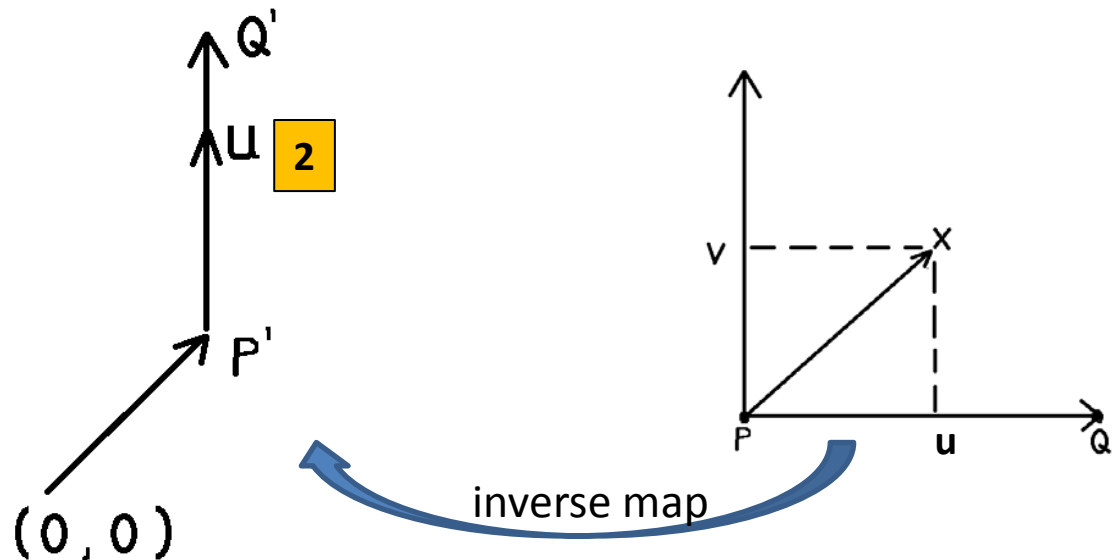
Using u and v , we now compute X'

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|}$$

$$= P' + u \cdot (P'Q') + v \left(\frac{\text{perpendicular}(P'Q')}{|P'Q'|} \right)$$

2

note: this is a unit vector

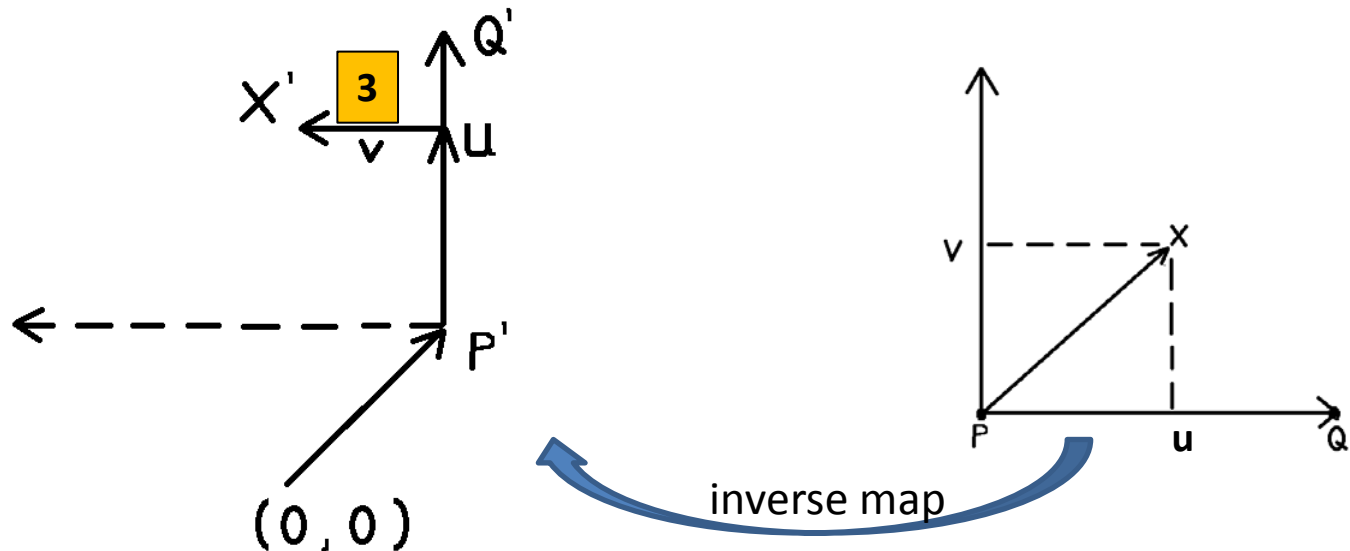


Walk-Thru

Using u and v , we now compute X'

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|}$$
$$= P' + u \cdot (P'Q') + v \left(\frac{\text{perpendicular}(P'Q')}{|P'Q'|} \right)$$

3



Finished: Transform with 1 Line Pair

For each pixel X in the destination image
find the corresponding u, v
find the X' in the source image for that u, v
 $\text{destinationImage}(X) = \text{sourceImage}(X')$

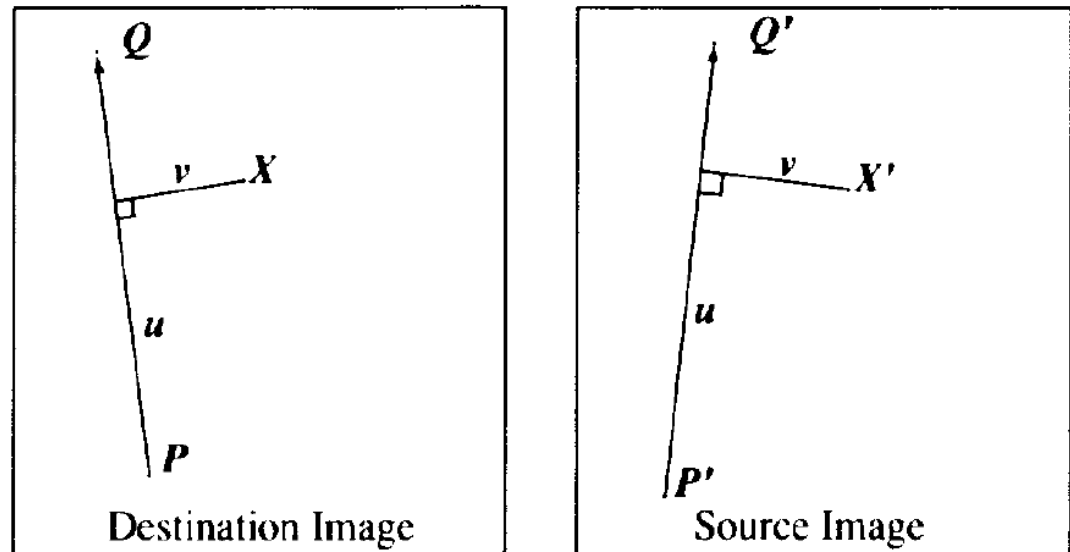


Figure 1: Single line pair

Results: Each Using One Pair of Lines

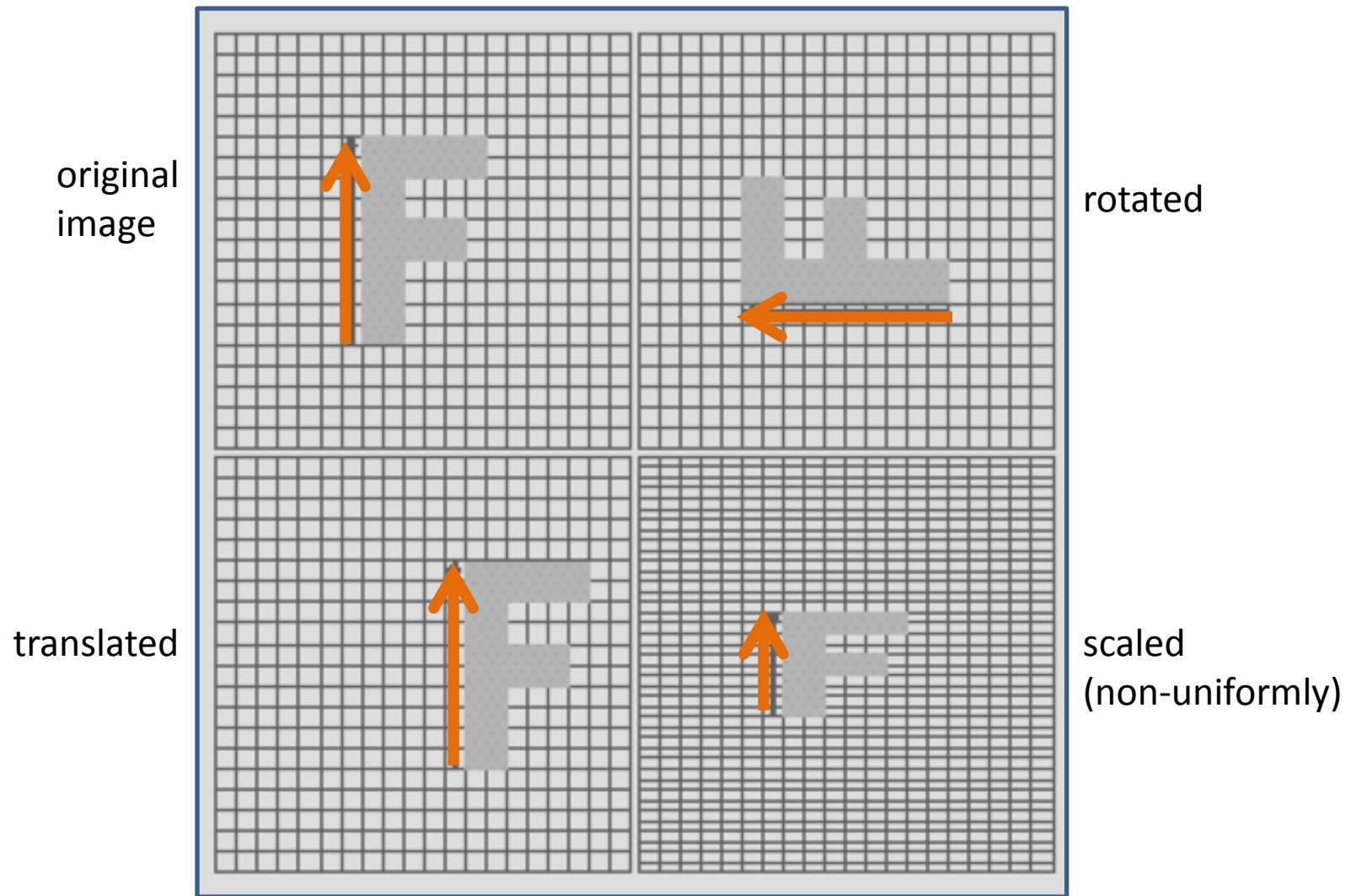


Figure 2: Single line pair examples

Transform with Multiple Line Pairs

- More complex and makes use of fields of influence from each line to identify which pixel X' in the source image that must be sampled for each pixel X in the destination image

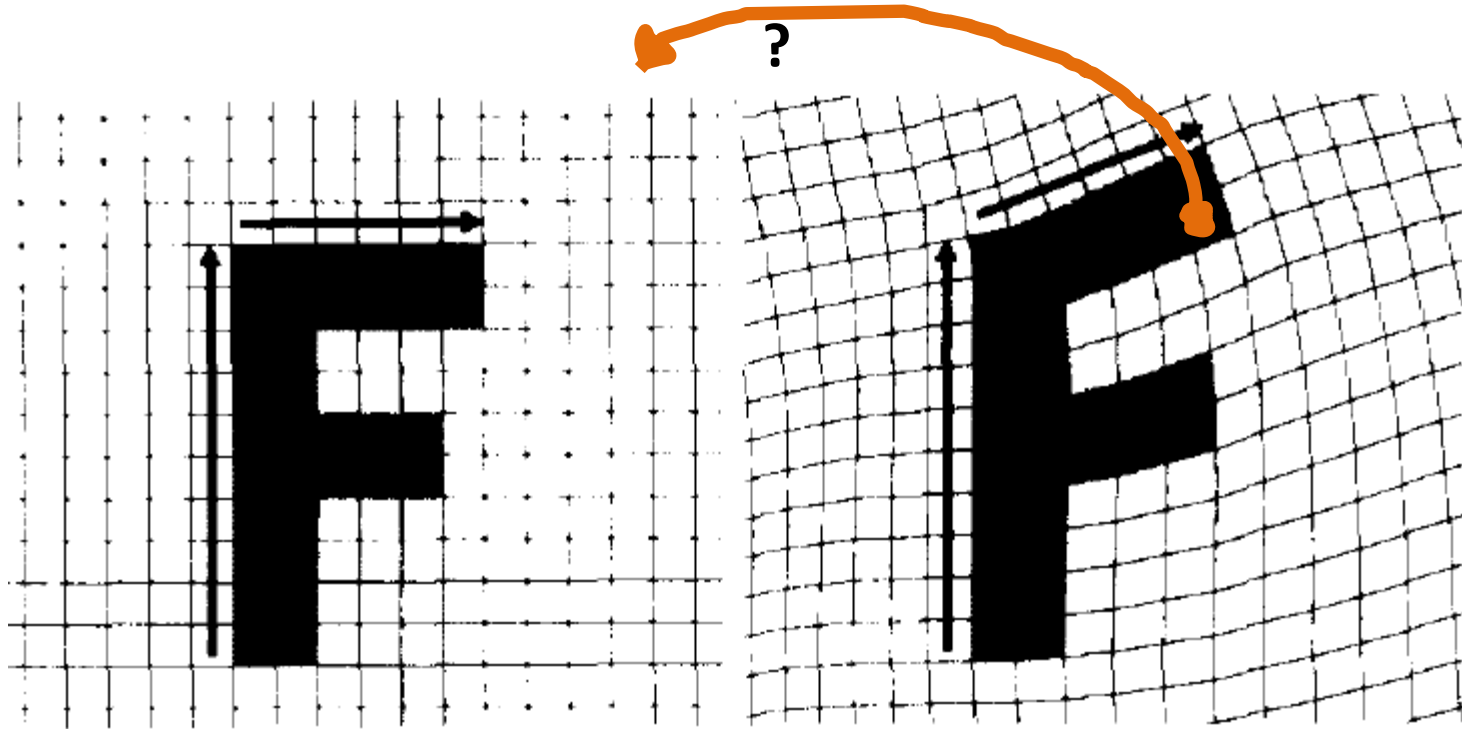
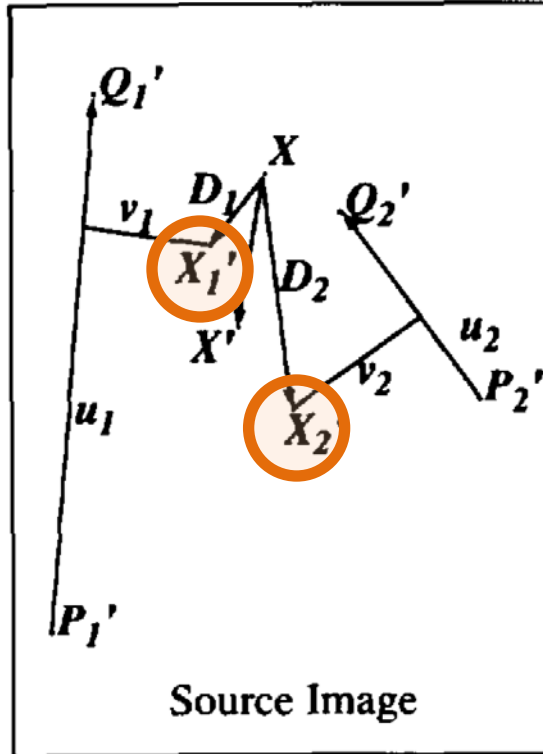
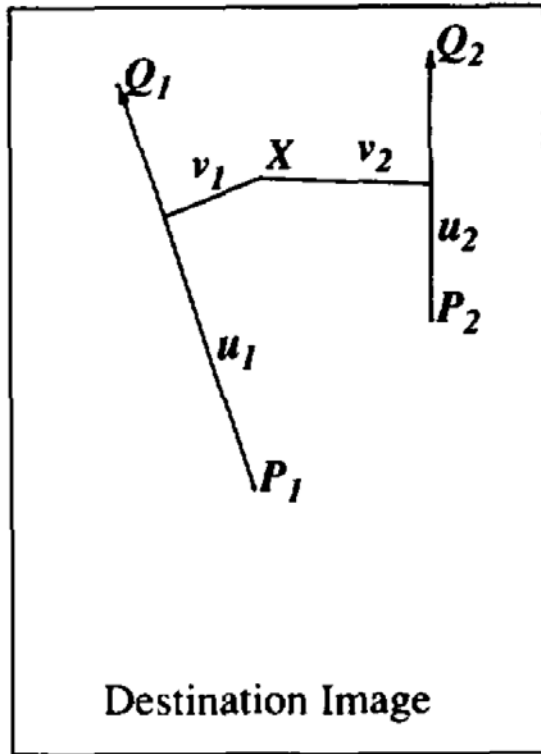


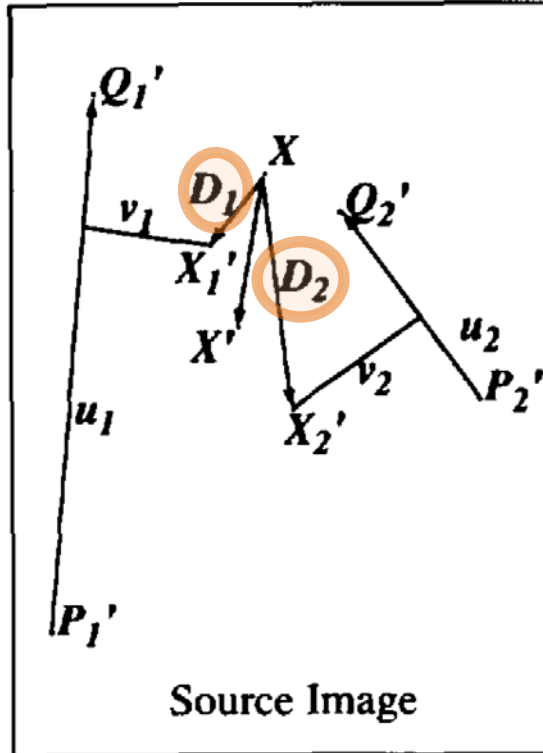
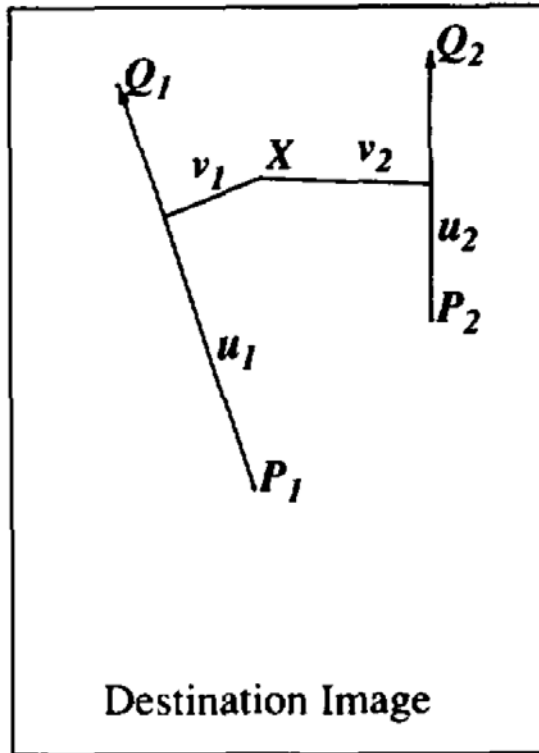
Figure 4: Multiple line pair example

Transform with Multiple Line Pairs



X'_i are obtained by
single line pairs

Transform with Multiple Line Pairs

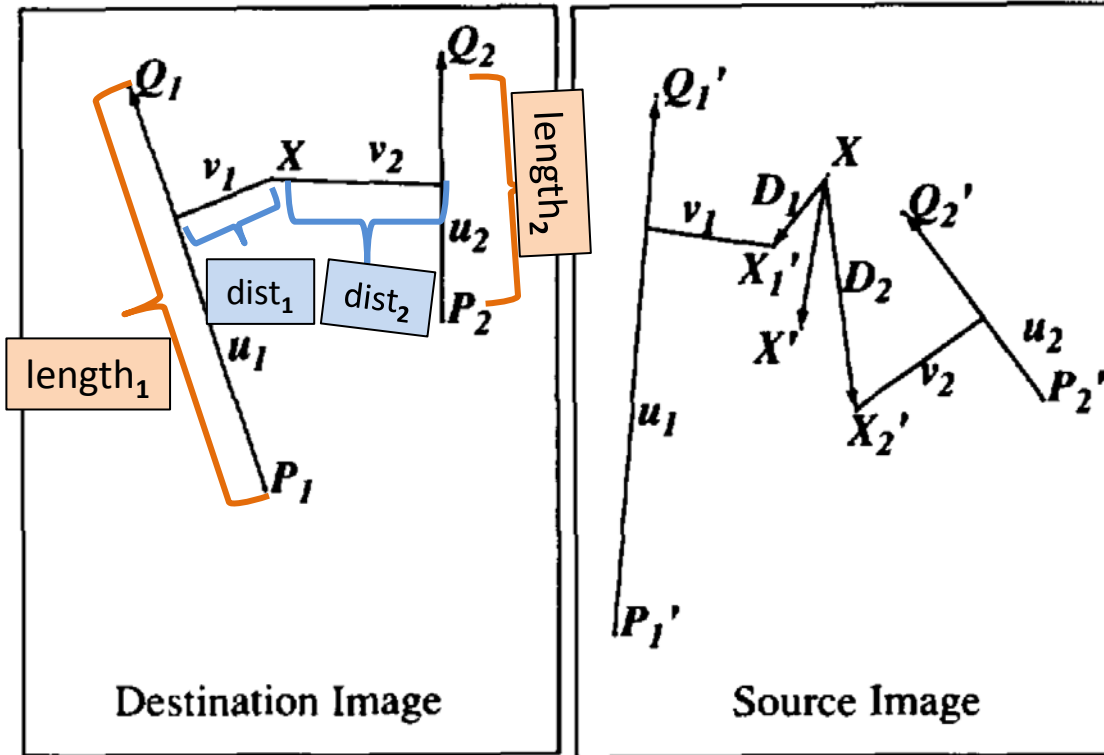


X'_i are obtained by
single line pairs

$$D_i = X'_i - X$$

displacement

Transform with Multiple Line Pairs



X'_i are obtained by
single line pairs

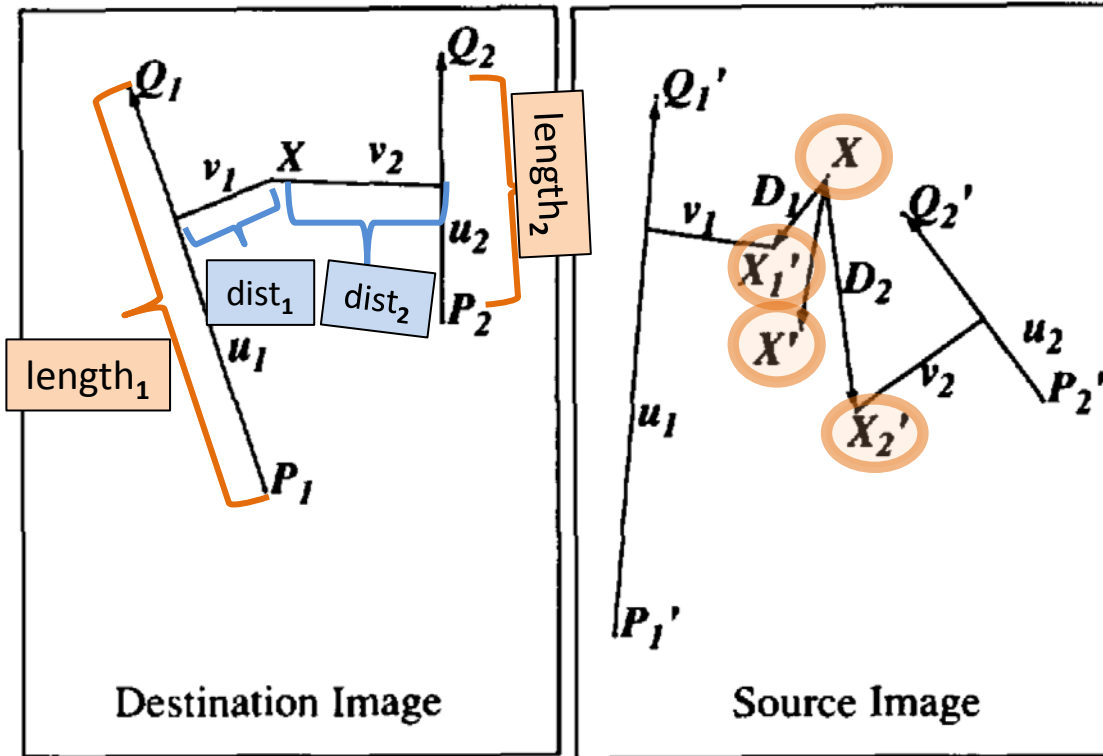
$$D_i = X'_i - X$$

displacement

$$weight_i = \left(\frac{(length_i)^p}{a + dist_i} \right)^b$$

a , p , and b
are constants that can be used
to change the relative effect
of the lines

Transform with Multiple Line Pairs



X'_i are obtained by
single line pairs

$$D_i = X'_i - X$$

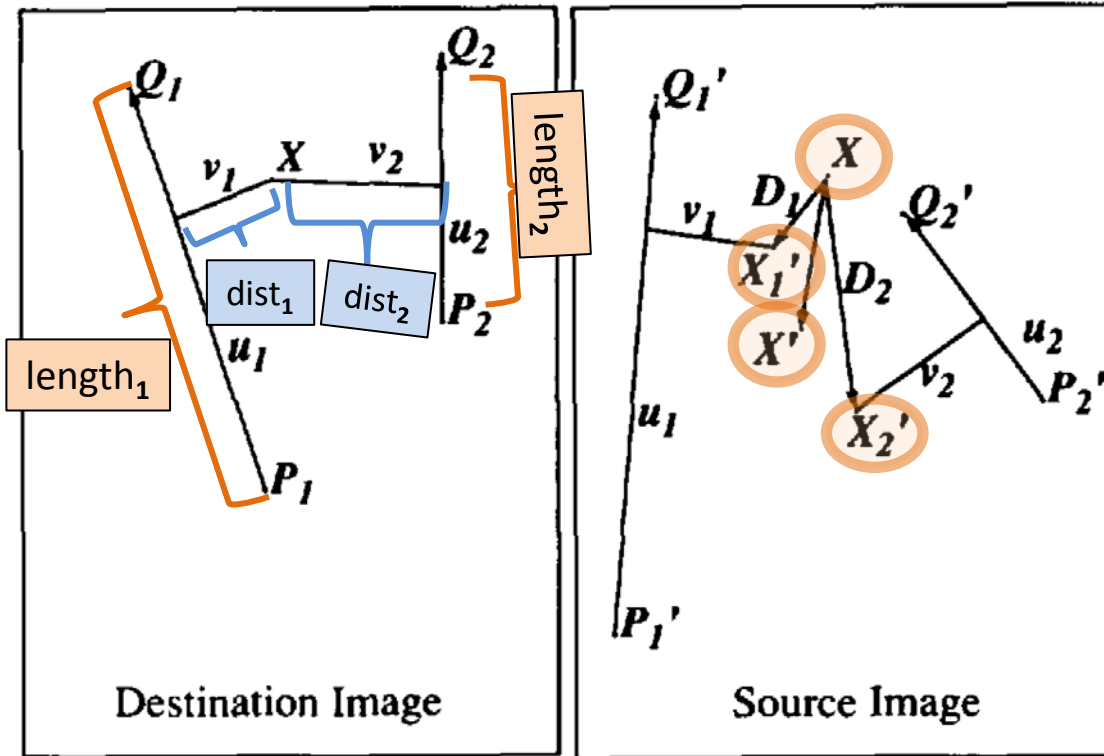
displacement

$$weight_i = \left(\frac{(length_i)^p}{a + dist_i} \right)^b$$

$a, p,$ and b
are constants that can be used
to change the relative effect
of the lines

$$X' = X + \frac{\sum (weight_i * D_i)}{\sum weight_i}$$

Transform with Multiple Line Pairs



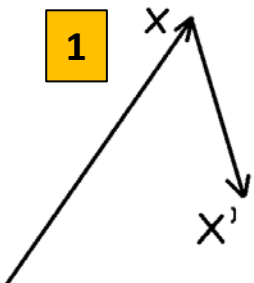
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single line pairs

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displacement

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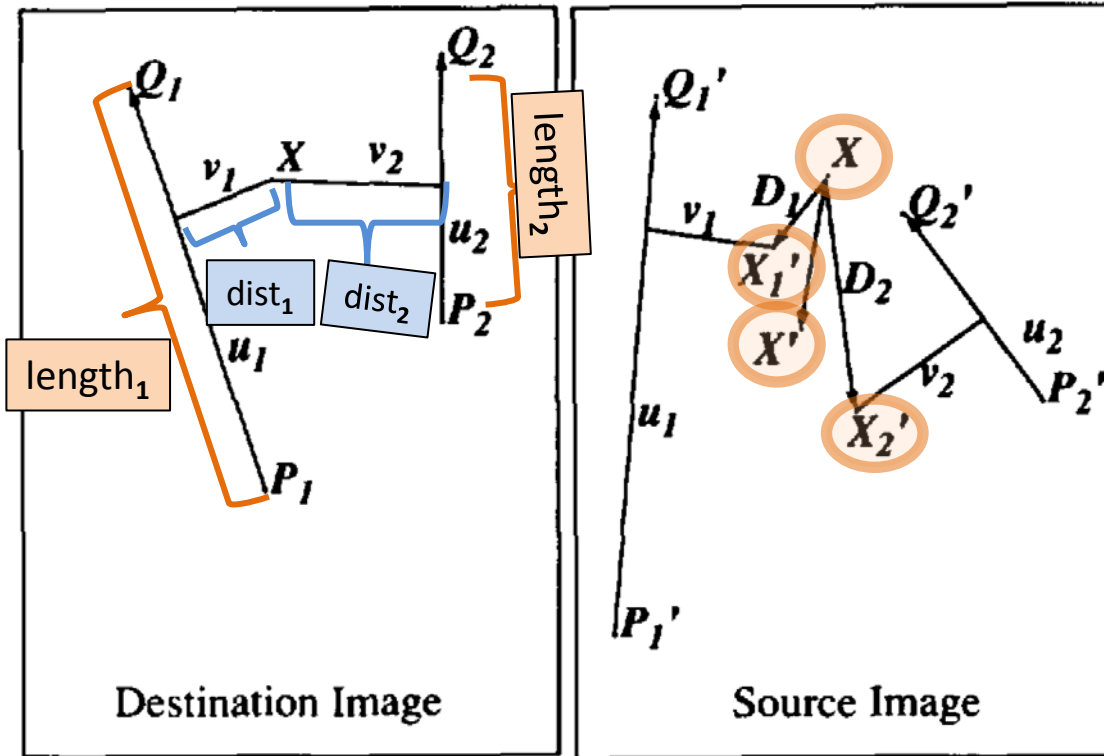
a, p, and b
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$$X' = X + \frac{\sum (weight_i * D_i)}{\sum weight_i}$$

1

Transform with Multiple Line Pairs



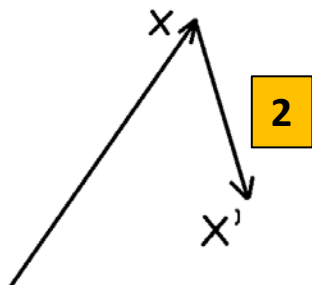
X'_i are obtained by
single line pairs

$$D_i = X'_i - X$$

displacement

$$weight_i = \left(\frac{(length_i)^p}{a + dist_i} \right)^b$$

a , p , and b
are constants that can be used
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of the lines

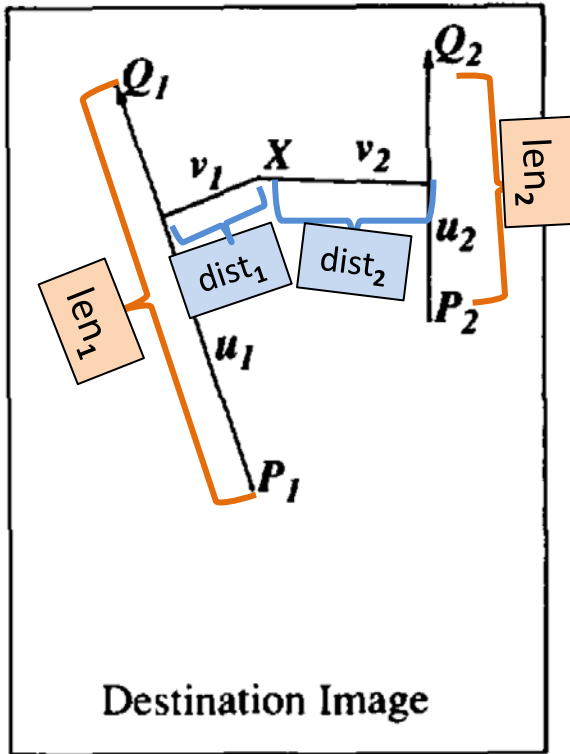


plus the weighted sum of D_i
(*displacement*)

$$X' = X + \frac{\sum (weight_i * D_i)}{\sum weight_i}$$

2

Constant Details



$$weight_i = \left(\frac{(len_i)^p}{a + dist_i} \right)^b$$

a – adjust the influence of distance; when a is larger, distance has smaller influence. When a is close to 0, pixels on a line go exactly to corresponding line as the line's influence is infinite.

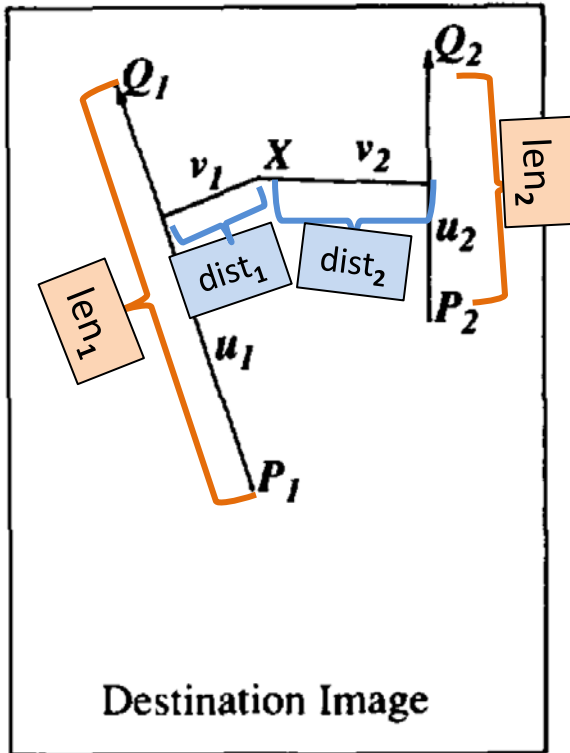
$$a + dist_i \rightarrow 0 \text{ then } weight_i \rightarrow \infty$$

b – adjust the influence of length/distance ratio; when b is larger, longer and nearer line has larger influence. When b is 0, all lines have the same influence on each pixel.

p – adjust the influence of length; when p is larger, longer lines have greater influence than shorter lines. When p is 0, different lengths have the same influence.

a, **p**, and **b** are constants that can be used to change the relative effect of the lines

Constant Details



$$weight_i = \left(\frac{(len_i)^p}{a + dist_i} \right)^b$$

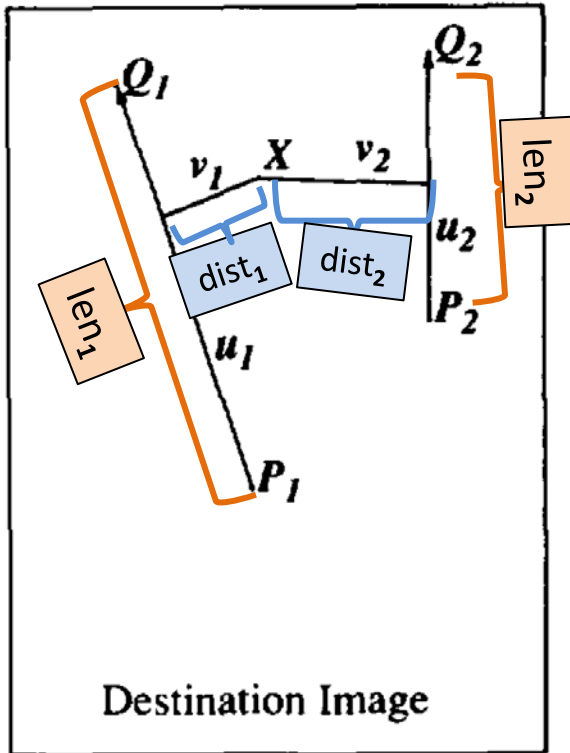
a – adjust the influence of distance; when a is larger, distance has smaller influence. When a is close to 0, pixels on a line go exactly to corresponding line as the line's influence is infinite.

b – adjust the influence of length/distance ratio; when b is larger, longer and nearer line has larger influence. When b is 0, all lines have the same influence on each pixel.

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a, **p**, and **b** are constants that can be used to change the relative effect of the lines

Constant Details



$$weight_i = \left(\frac{(len_i)^p}{a + dist_i} \right)^b$$

a – adjust the influence of distance; when a is larger, distance has smaller influence. When a is close to 0, pixels on a line go exactly to corresponding line as the line's influence is infinite.

b – adjust the influence of length/distance ratio; when b is larger, longer and nearer line has larger influence. When b is 0, all lines have the same influence on each pixel.

p – adjust the influence of length; when p is larger, longer lines have greater influence than shorter lines. When p is 0, different lengths have the same influence.

a, **p**, and **b** are constants that can be used to change the relative effect of the lines

Pseudocode: Multiple Line Pairs

For each pixel X in the destination

$DSUM = (0,0)$

$weightsum = 0$

For each line $P_i Q_i$

calculate u, v based on $P_i Q_i$

calculate X'_i based on u, v and $P_i' Q_i'$

calculate displacement $D_i = X'_i - X$ for this line

$dist =$ shortest distance from X to $P_i Q_i$

$weight = (length_p / (a + dist))b$

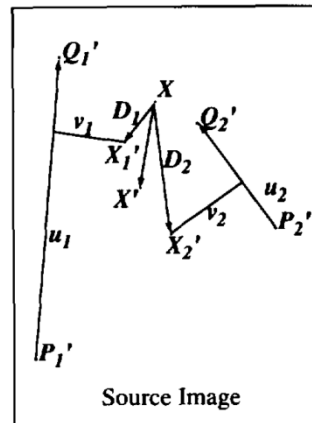
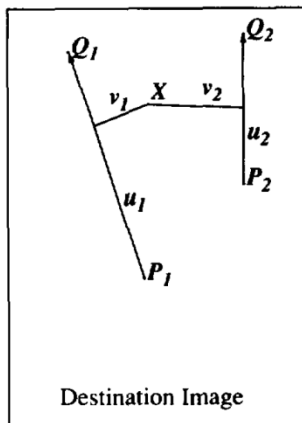
$DSUM += D_i * weight$

$weightsum += weight$

$X' = X + DSUM / weightsum$

$destinationImage(X) = sourceImage(X')$

$$X' = X + \frac{\sum (weight_i * D_i)}{\sum weight_i}$$



Results with Multiple Line Pairs

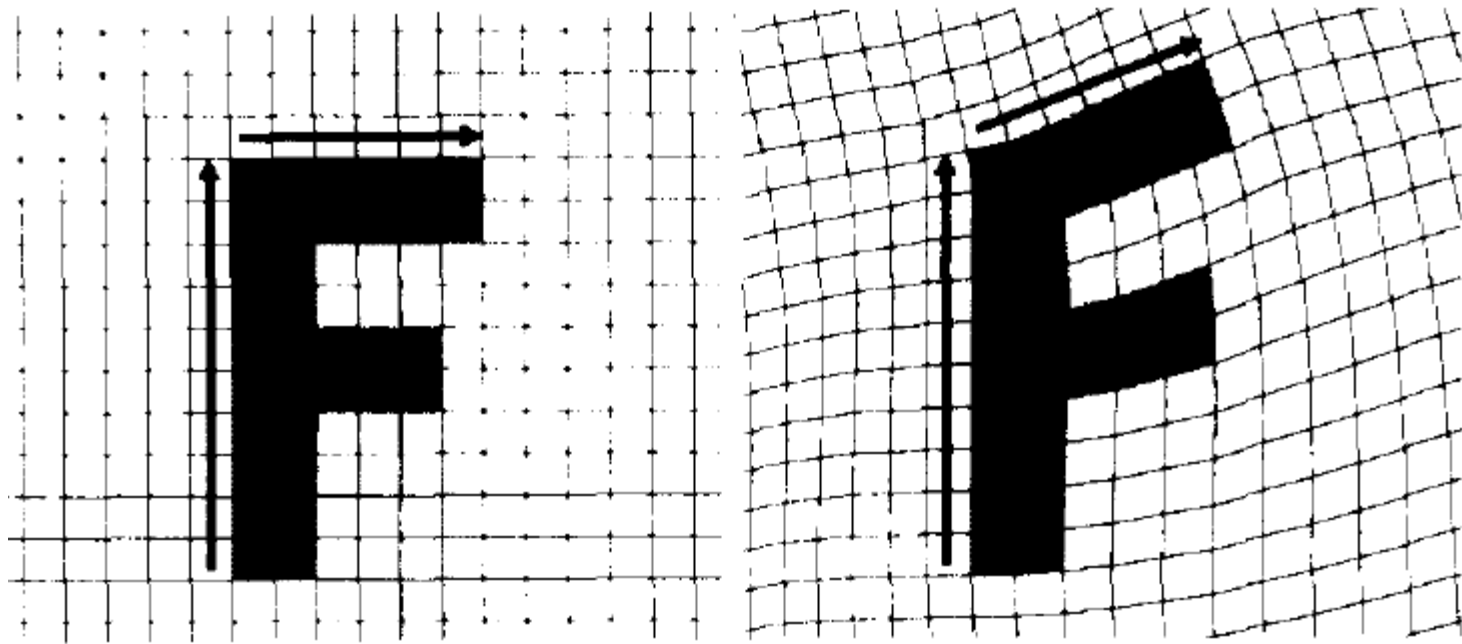
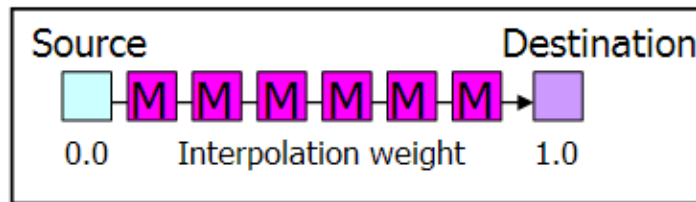
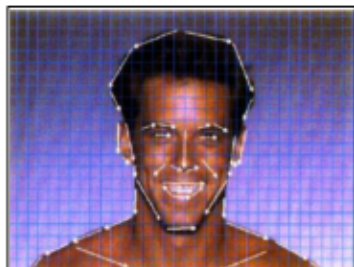


Figure 4: Multiple line pair example

Morphing Between 2 Still Images



Source



Source

Warp Source →



this is what we just talked about doing

Interpolate lines to create new lines of intermediate frame.



Destination

Destination

Warp Source →

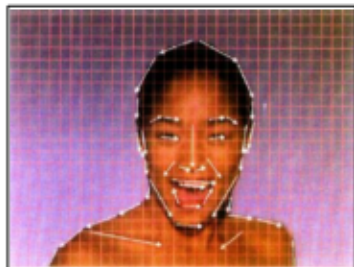


Blend



Subjects of images now have same geometry.

Destination



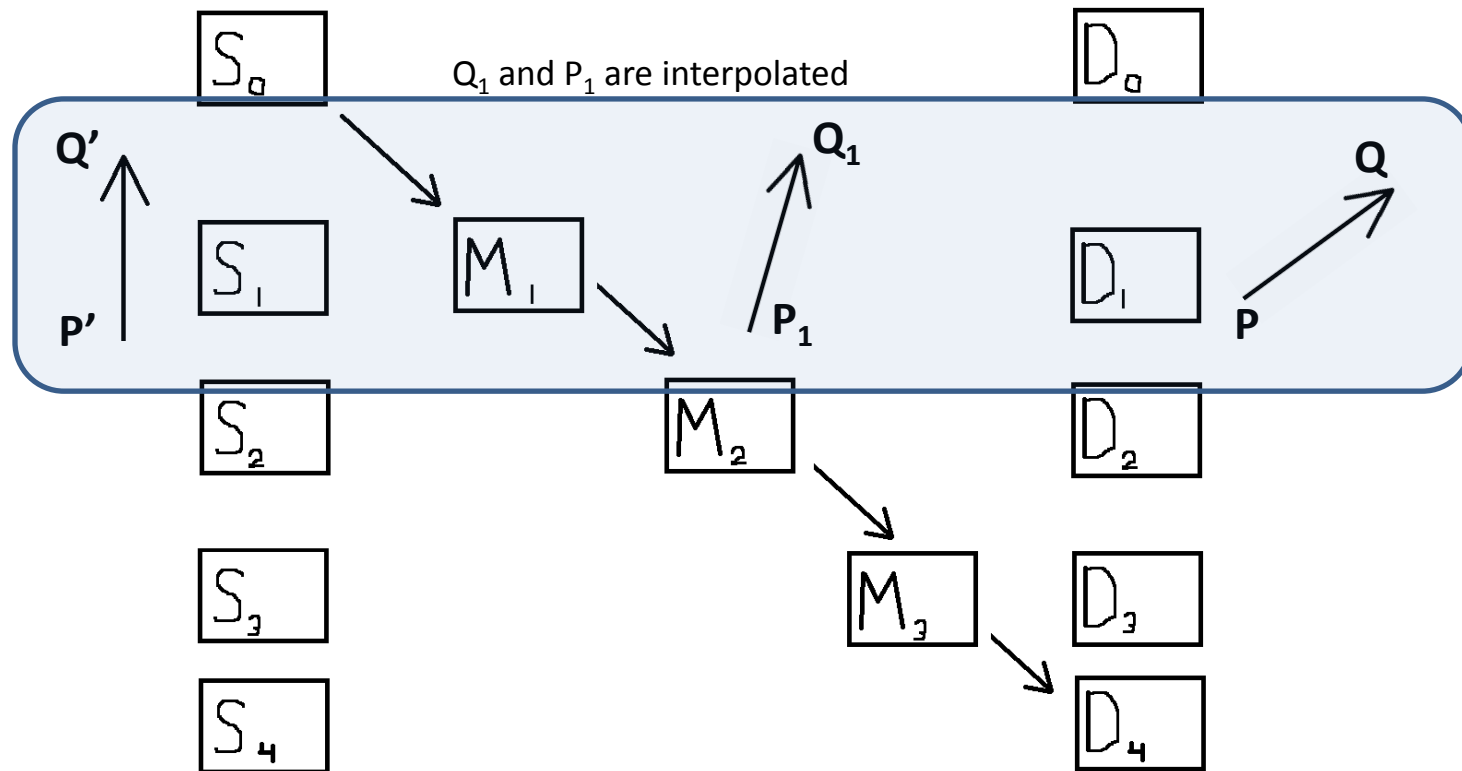
Animated Sequences



Specify lines on keyframes and interpolate lines on other frames

Example:

$S_{1.5}$, $D_{1.5}$ would be interpolated between Q_1 , P_1 and Q_2 , P_2 .



Note:

Interpolation can be

1. on the end points of line pairs

OR

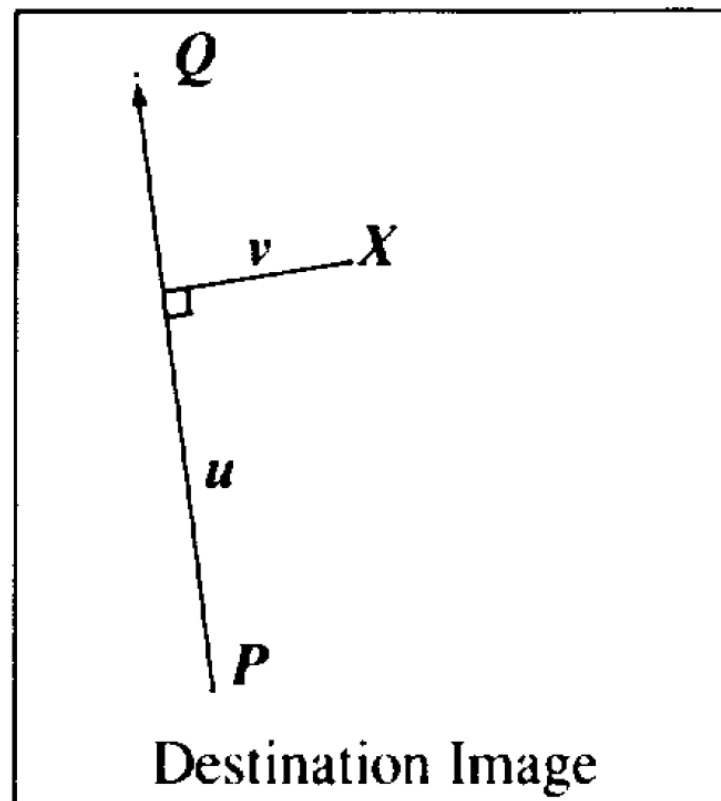
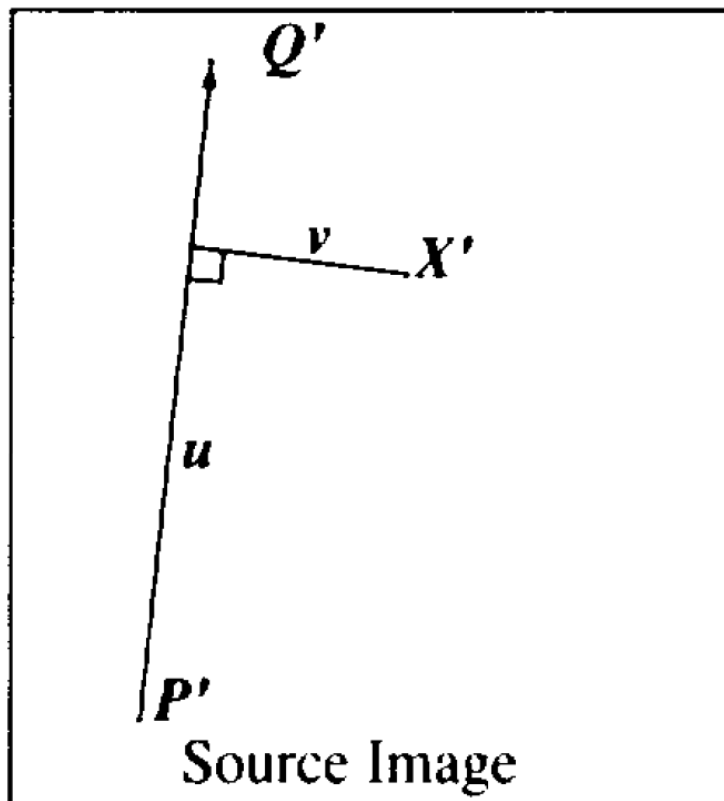
2. on the center, orientation and length of line pairs

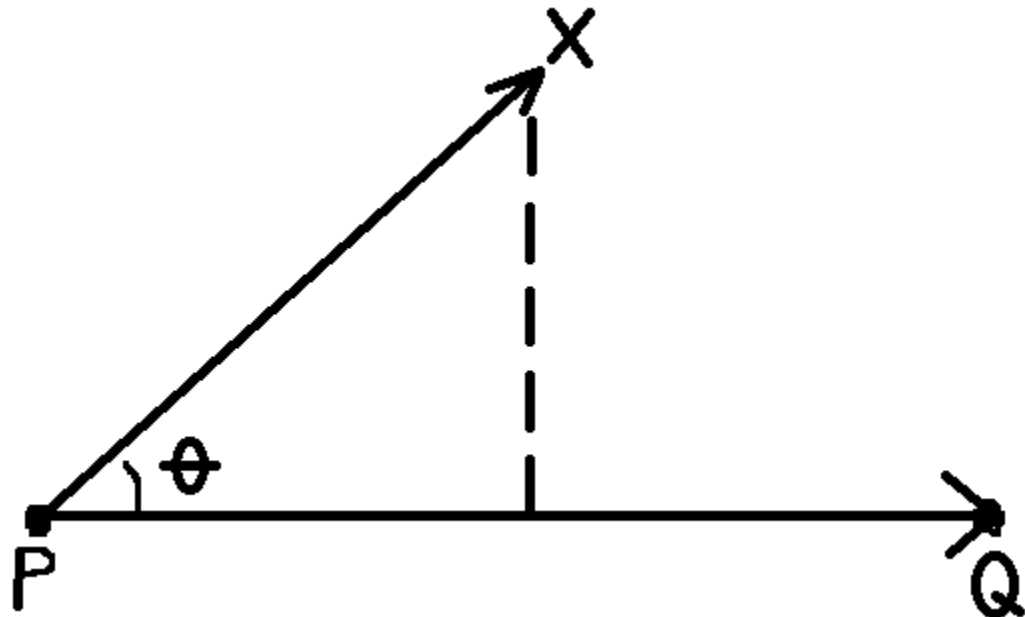
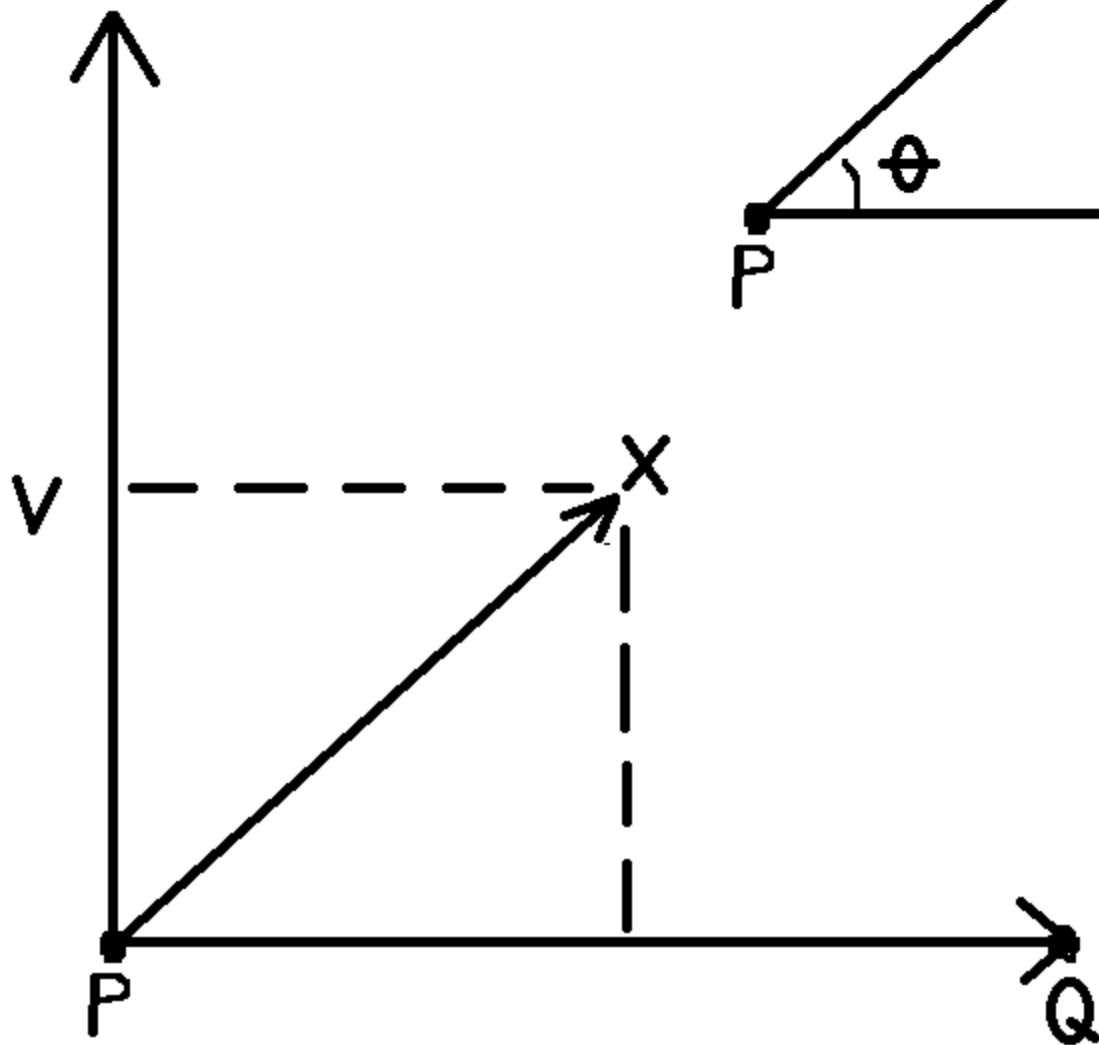
Questions?

- Beyond D2L
 - Examples and information can be found online at:
 - *<http://docdingle.com/teaching/cs.html>*

- *Continue to more stuff as needed*

Extra Reference Stuff Follows





S_0

D_0



S_1

M_1

D_1



S_2

M_2

D_2



S_3

M_3

D_3



S_4

D_4

Credits

- Much of the content derived/based on slides for use with the book:
 - *Digital Image Processing*, Gonzalez and Woods
- Some layout and presentation style derived/based on presentations by
 - Donald House, Texas A&M University, 1999
 - Bernd Girod, Stanford University, 2007
 - Shreekanth Mandayam, Rowan University, 2009
 - Igor Aizenberg, TAMUT, 2013
 - Xin Li, WVU, 2014
 - George Wolberg, City College of New York, 2015
 - Yao Wang and Zhu Liu, NYU-Poly, 2015
 - Sinisa Todorovic, Oregon State, 2015

