## Digital Image Processing Edge Detection: Smart Scissors



## Lecture Objectives

- Previously
- Filtering
- Interpolation Image Manipulation
- Warping
- Morphing
- Compression Image Compression
- Edge Detection
- Today

Image Analysis

- Intelligent Scissors


## Recall: Edge Detection



- Goal: Identify sudden changes (discontinuities) in an image
- Much of the 'shape' information of the image can be realized in the edges
- Ideal Result: an artist's line drawing
- aside: who can use knowledge beyond a single image


## Recall: Canny Edge Detector

- Filter image with derivative of Gaussian

- Find magnitude and orientation of gradient
- Apply non-maximum suppression
- Linking and thresholding (hysteresis)
- Define 2 thresholds: low and high
- Use the high threshold to start edge curves and the low threshold to continue them


## Extracting Objects



- How can the tiger be extracted from the image?
- Difficult to do manually
- Difficult to do automatically (but possible)
- Easier to do semi-automatically


## Paper to Read/Reference

- Intelligent Scissors, Mortensen et. al, SIGGRAPH 1995


## Intelligent Scissors



Figure 2: Image demonstrating how the live-wire segment adapts and snaps to an object boundary as the free point moves (via cursor movement). The path of the free point is shown in white. Live-wire segments from previous free point positions ( $t_{0}, t_{1}$, and $t_{2}$ ) are shown in green.

## Intelligent Scissors

- Question
- How do we find a path from seed to mouse that follows an object boundary as closely as possible?
- Answer
- Define a path that stays as close as possible to edges



## Intelligent Scissors

- Basic Idea
- Define edge score for each pixel
- assign edge pixels a low score
- Find lowest cost path from seed to mouse



## Let's look at this more closely

- Treat the image as a graph

Graph

- node for every pixel p

- link between every adjacent pair of pixels, p,q
- cost c for each link

Note: each link has a cost

- this is a little different than the figure before where each pixel had a cost


## Defining the costs



Want to hug image edges: how to define cost of a link?

- good (low-cost) links follow the intensity edge
- want intensity to change rapidly $\perp$ to the link
- $c \approx-\frac{1}{\sqrt{2}}$ |intensity of $r$ - intensity of $s \mid$


## Defining the costs



- c can be computed using a cross-correlation filter
- assume it is centered at $p$


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A couple more modifications

- Scale the filter response by length of link c. Why?
- Make c positive
- Set c = (max-|filter response|*length)
- where max $=$ maximum |filter response|*length over all pixels in the image ${ }_{\text {source: Noah Snavely }}$


## Dijkstra's shortest path algorithm



## Algorithm

1. init node costs to $\infty$, set $p=$ seed point, $\operatorname{cost}(p)=0$
2. expand $p$ as follows:
for each of p's neighbors $q$ that are not expanded

$$
\text { set } \operatorname{cost}(q)=\min \left(\operatorname{cost}(p)+c_{p q}, \operatorname{cost}(q)\right)
$$

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put $q$ on the ACTIVE list (if not already there)

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3. set $r=$ node with minimum cost on the ACTIVE list
4. repeat Step 2 for $p=r$

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## Dijkstra's shortest path algorithm

- Properties
- It computes the minimum cost path from the seed to every node in the graph. This set of minimum paths is represented as a tree
- Running time, with $N$ pixels:
- $\mathrm{O}\left(\mathrm{N}^{2}\right)$ time if you use an active list
- $\mathrm{O}(\mathrm{N} \log \mathrm{N}$ ) if you use an active priority queue (heap)
- takes fraction of a second for a typical (640x480) image
- Once this tree is computed once, we can extract the optimal path from any point to the seed in $\mathrm{O}(\mathrm{N})$ time.
- it runs in real time as the mouse moves
- What happens when the user specifies a new seed?


## Questions?

- Beyond D2L
- Examples and information can be found online at:
- http://docdingle.com/teaching/cs.html
- Continue to more stuff as needed


## Extra Reference Stuff Follows

## Credits

- Much of the content derived/based on slides for use with the book:
- Digital Image Processing, Gonzalez and Woods
- Some layout and presentation style derived/based on presentations by
- Donald House, Texas A\&M University, 1999
- Sventlana Lazebnik, UNC, 2010
- Noah Snavely, Cornell University, 2012
- Xin Li, WVU, 2014
- George Wolberg, City College of New York, 2015
- Yao Wang and Zhu Liu, NYU-Poly, 2015



