

Section 4.2

Solutions and Hints

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for the book:

Precalculus, Mathematics for Calculus 4th Edition
by James Stewart, Lothar Redlin and Saleem Watson.

22. Evaluate the given expression.

22 a. $\log_4 (2^{1/2})$

$$\begin{aligned}\log_4 \sqrt{2} &= \log_4(2^{1/2}) && \text{since the base is 4} \\ &= \log_4((4^{1/2})^{1/2}) && \text{getting everything in terms of 4} \\ &= \log_4(4^{1/4}) && \text{is a good idea} \\ &= (1/4) * \log_4(4) \\ &= (1/4) * 1 && \text{because stuff will cancel nicely} \\ &= \mathbf{1/4}\end{aligned}$$

22 b. $\log_4 (1/2)$

$$\begin{aligned}\log_4(1/2) &= \log_4(2^{-1}) \\ &= \log_4((4^{1/2})^{-1}) \\ &= \log_4(4^{-1/2}) \\ &= - 1/2 \log_4(4) \\ &= - 1/2 * 1 \\ &= \mathbf{- 1/2}\end{aligned}$$

22 c. $\log_4 (8)$

If you haven't seen the pattern, solve $8 = 4^k$ first and then substitute stuff in.
It goes like this:

$$8 = 4 * 2 = 4 * 4^{1/2} = 4^{3/2}$$

So

$$\log_4(8) = \log_4(4^{3/2}) = \mathbf{3/2}$$

30 a. Solve for x: $\log_x (6) = 1/2$

$$\begin{aligned}\log_x(6) = 1/2 &\rightarrow x^{\log_x 6} = x^{1/2} \\ &\rightarrow 6 = x^{1/2} \\ &\rightarrow \mathbf{36 = x}\end{aligned}$$

This works because if $a = b$ then $x^a = x^b$
Now square both sides

30 b. Solve for x: $\log_x (3) = 1/3$

$$\begin{aligned}\log_x(3) = 1/3 &\rightarrow x^{\log_x 3} = x^{1/3} \\ &\rightarrow 3 = x^{1/3} \\ &\rightarrow \mathbf{27 = x}\end{aligned}$$

Now cube both sides

60. Find the domain of $g(x) = \ln(x - x^2)$

Recall the domain of a function is the allowable x values of the function, $g(x)$.
Recall that you can only take the log (or natural log) of non-negative numbers.
So solve $x - x^2 \geq 0$

$$x - x^2 \geq 0 \quad \rightarrow x(1 - x) \geq 0$$

Notice $x*(1 - x) = 0$ at $x = 0$ and $x = 1$. So use a sign table to solve:

	$(-\infty, 0)$	0	$(0, 1)$	1	$(1, \infty)$
sign of x	-	0	+	+	+
sign of $(1 - x)$	+	+	+	0	-
sign of $x * (1 - x)$	-	0	+	+	-

So the domain is whatever intervals make $x * (1 - x)$ non-negative.

Domain = $[0, 1]$