

Section 5.3

Solutions and Hints

by Brent M. Dingle

for the book:

Precalculus, Mathematics for Calculus 4th Edition
by James Stewart, Lothar Redlin and Saleem Watson.

50. A tuning fork is struck producing a pure tone as its tines vibrate. The vibrations are modeled by the function:

$$v(t) = 0.7 \sin(880\pi t)$$

where $v(t)$ is the displacement of the tines in millimeters at time t seconds.

50a. Find the period of the vibration.

You will first want to write $v(t)$ in the form of $v(t) = y = a \sin(k(t - b))$

$$v(t) = 0.7 \sin(880\pi t) = 0.7 \sin(880\pi * (t - 0))$$

Thus amplitude = $a = 0.7$ millimeters

period = $2\pi / k = 2\pi / (880\pi) = (1/440)$ seconds (≈ 0.00227 seconds)

phase shift = $b = 0$

Of course all you need is **period = (1 / 440) seconds.**

50b. Find the frequency of the vibration

(i.e. the number of times the fork vibrates per second).

For this all you need to remember is that frequency = $1 / \text{period}$.

Thus the frequency = $1 / (1 / 440) = \mathbf{440 \text{ vibrations per second.}}$

50c. Graph the function $v(t)$.

This is left for you to complete – use your calculator.