

Section 3.8

Solutions and Hints

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for the book:
Calculus, Early Vectors
by James Stewart.

38. Given $s(t) = 2t^3 - 7t^2 + 4t + 1$ represents the position of a particle at time t . Find equations for the velocity and acceleration in terms of t . Calculate the acceleration at $t = 1$. Find the particle's acceleration at times when its velocity is zero.

To find the velocity and acceleration equations means we must find the first and second derivatives of position:

$$\begin{aligned} s(t) &= 2t^3 - 7t^2 + 4t + 1 \\ v(t) = s'(t) &= 6t^2 - 14t + 4 \\ a(t) = s''(t) &= 12t - 14 \end{aligned}$$

Finding the acceleration at $t = 1$ is just putting 1 into $a(t)$:
 $a(1) = 12 \cdot 1 - 14 = -2$

The particle's acceleration at time = 1 sec is -2 .

For the last question we must set $v(t) = 0$ and solve for t . We will then put those times into $a(t)$.

$$\begin{aligned} 6t^2 - 14t + 4 &= 0, && \text{divide everything by 2.} \\ 3t^2 - 7t + 2 &= 0, && \text{factor.} \\ (3t - 1)(t - 2) &= 0 \end{aligned}$$

So at $t = 1/3$ and $t = 2$ the particle's velocity is zero.
 $a(1/3) = 12 \cdot (1/3) - 14 = -10$ and $a(2) = 12 \cdot 2 - 14 = 10$

At times $t = 1/3$ and 2 velocity is zero and acceleration is -10 and 10 , respectively.

46. Find the acceleration at the given value of t:

$$\mathbf{r}(t) = \langle 4\cos(t), 3\sin(t) \rangle \quad \text{at } t = \pi/3$$

$$\text{velocity} = \mathbf{r}'(t) = \langle -4\sin(t), 3\cos(t) \rangle$$

$$\text{acceleration} = \mathbf{r}''(t) = \langle -4\cos(t), -3\sin(t) \rangle$$

$$\begin{aligned} \mathbf{r}''(\pi/3) &= \langle -4\cos(\pi/3), -3\sin(\pi/3) \rangle \\ &= \langle -2, \frac{-3\sqrt{3}}{2} \rangle \end{aligned}$$

The acceleration at $t = \pi/3$ is

$$\langle -2, \frac{-3\sqrt{3}}{2} \rangle.$$